

Measuring systemic risk: The Indirect Contagion Index

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Based on: Rama Cont and Eric Schaanning (2016) Measuring systemic risk: The Indirect Contagion Index

- 1 Endogenous risk and price-mediated contagion
- **2** Modeling fire sales
- 3 Monitoring systemic risk: The Indirect Contagion Index

4 Scenario design



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- So: B experiences a loss following a large shock to the illiquid asset: B has an (indirect) exposure to an asset it does not hold!
- Magnitude of this indirect exposure is directly linked to the overlap between B and institutions holding this asset.
- Large diversified institutions increase overlaps across system and become nodes for price-mediated contagion.

Losses arising from indirect exposures



Figure: Losses of HSBC and Banco Santander as a function of losses in the Southern European real estate sector.

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- Given institutions' portfolio holdings, are the stress scenarios that we consider the right ones?
- How can we **quantify** the notion of "interconnectedness" for Global systemically important banks (GSIBs)?
- Can regulators disseminate a metric that would allow institutions to quantify their exposures to price-mediated contagion?

Bank stress tests and interconnectedness assessments

- Bank stress tests have become an essential component of bank supervision (EU-wide EBA stress tests, Dodd-Frank tests (DFAST, CCAR)).
- *Static balance sheet assumption*: Stress tests assume 'passive' behaviour by banks.
- BCBS 2015: "Stress tests conducted by bank supervisors still lack a genuine macro-prudential component": "*endogenous reactions* to initial stress, loss amplification mechanisms and *feedback effects*" are missing.
- Currently *"interconnectedness"* in the GSIB methodology is based on (i) intra-financial system assets, (ii) intra-financial system liabilities, (iii) securities outstanding.

Channels of loss amplification in the financial system

- Counterparty Risk: balance sheet contagion through asset devaluation
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- **Feedback effects from fire sales**: loss contagion through mark-to-market losses in common asset holdings

Research on financial networks and their use in macroprudential regulation has focused on direct contagion mechanisms (1+2). Regulatory measures have focused on 1 (large exposure limits, central clearing, CVA, ring-fencing) or 2 (LCR, NSFR).

Modeling fire sales

Ingredients:

• Data: Portfolio holdings of financial institutions by asset class: N institutions, K illiquid asset classes, M marketable asset classes $\rightarrow N \times (M + K)$ portfolio matrix (network)

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- Mark-to-market accounting: transmits market impact to all institutions → may lead to feedback if market losses large

Balance sheets: illiquid and marketable assets

Illiquid assets
Residential mortgage exposures
Commercial real estate exposure
Retail exposures: Revolving credits, SME, Other
Indirect sovereign exposures in the trading book
Defaulted exposures
Residual exposures
Marketable assets
Corporate bonds
Sovereign debt
Derivatives
Institutional client exposures: interbank, CCPs,

Table: Stylized representation of asset classes in bank balance sheets. (Data: European Banking Authority)

- Illiquid holdings of institution $i: \Theta^i := \sum_{\kappa=1}^K \Theta^{i\kappa}$.
- Marketable Securities held by $i: \Pi^i := \sum_{\mu=1}^M \Pi^{i\mu}$.
- Equity (Tier 1 capital): Cⁱ

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- Financial institutions are subject to various **one-sided** portfolio constraints: leverage ratio, capital ratio, liquidity ratio.
- Leverage ratio of *i*:

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- A stress scenario is defined by a vector ε ∈ [0,1]^K whose components ε_κ are the percentage shocks to asset class κ.
- Initial/Direct loss of portfolio *i*: $L^{i}(\epsilon) = \epsilon . \Theta^{i} = \sum_{\kappa} \Theta^{i\kappa} \epsilon_{\kappa}$

Deleveraging

Deleveraging assumption: if following a loss L^i in asset values the leverage of bank *i* exceeds the constraint

$$\lambda^i = rac{\Theta^i + \Pi^i - L^i}{C^i - L^i} > \lambda_{\max}$$

bank deleverages by selling a proportion $\Gamma^i \in [0, 1]$ of assets in order to restore a leverage ratio $\lambda_b^i \leq \lambda_{max}$:

$$\frac{(1-\Gamma^{i})\Pi^{i}+\Theta^{i}-L^{i}}{C^{i}-L^{i}}=\lambda_{b}^{i}\leq\lambda_{\max}\quad\Rightarrow\Gamma^{i}=\frac{C^{i}(\lambda^{i}-\lambda_{b}^{i})}{\Pi^{i}}\mathbf{1}_{\lambda^{i}>\lambda_{\max}}$$

Develeraging in response to a loss



Figure: Percentage of marketable asset deleveraged in response to a shock to assets (circles) for a leverage constraint of 20. Leverage targeting (dotted blue) would lead to a linear response.

Measuring systemic risk

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Market impact function



Market impact function and market depth

The impact of a total distressed liquidation volume q is modelled by a *level-dependent market impact function*

$$\Psi_{\mu}(q,S) = \left(1 - rac{B_{\mu}}{S}
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where

$$D_{\mu} = c rac{ADV_{\mu}}{\sigma_{\mu}} \sqrt{ au},$$

- $S \geq B_{\mu}$ where B_{μ} is the price-floor
- ADV: average daily volume, σ_{μ} : daily volatility of asset
- $c \approx 0.25$, a coefficient to make Ψ_{μ} consistent with empirical estimates of the linear impact model for small volumes q.
- τ is the liquidation horizon

Estimated market depth



Market impact and feedback effects

Total liquidation in asset μ at k-th round: $q^{\mu} = \sum_{i=1}^{N} \prod_{k=1}^{j,\mu} \Gamma_{k}^{j,\mu}$

$$ext{Market impact}: \quad rac{\Delta S^\mu}{S^\mu} = - \Psi_\mu(q^\mu),$$

Impact/ inverse demand function: $\Psi_{\mu} > 0, \Psi'_{\mu} > 0, \Psi_{\mu}(0) = 0.$

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Impact/ inverse demand function: $\Psi_{\mu} > 0, \Psi'_{\mu} > 0, \Psi_{\mu}(0) = 0.$ Price move at k-th iteration of fire sales:

$$S_{k+1}^{\mu} = S_k^{\mu} \left(1 - \Psi_{\mu} \left(\sum_{j=1}^{N} \Pi_k^{j,\mu} \Gamma_{k+1}^j
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Measuring systemic risk

Fire sales losses

• Mark to market loss:

$$\begin{split} M_{k+1}^{i} &:= \sum_{\mu=1}^{M} \left((1 - \Gamma_{k+1}^{i}) \Pi_{k}^{i\mu} - \Pi_{k+1}^{i\mu} \right) \\ &= (1 - \Gamma_{k+1}^{i}) \sum_{\mu=1}^{M} \Pi_{k}^{i\mu} \Psi_{\mu} \left(\sum_{j=1}^{N} \Pi_{k}^{j\mu} \Gamma_{k+1}^{j} \right) \end{split}$$
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• Realised loss (implementation shortfall / slippage):

$$R_{k+1}^{i} := \alpha \Gamma_{k+1}^{i} \sum_{\mu=1}^{M} \Pi_{k}^{i\mu} \Psi_{\mu} \left(\sum_{j=1}^{N} \Pi_{k}^{j\mu} \Gamma_{k+1}^{j} \right)$$

Fire sales losses

• Mark to market loss:

$$\begin{split} M^{i}_{k+1} &:= \sum_{\mu=1}^{M} \left((1 - \Gamma^{i}_{k+1}) \Pi^{i\mu}_{k} - \Pi^{i\mu}_{k+1} \right) \\ &= (1 - \Gamma^{i}_{k+1}) \sum_{\mu=1}^{M} \Pi^{i\mu}_{k} \Psi_{\mu} \left(\sum_{j=1}^{N} \Pi^{j\mu}_{k} \Gamma^{j}_{k+1} \right) \end{split}$$

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• Fire sales loss:

$$L_k^i = (1 - (1 - \alpha)\Gamma_{k+1}^i) \sum_{\mu=1}^M \Pi_k^{i\mu} \Psi_\mu \left(\sum_{j=1}^N \Pi_k^{j\mu} \Gamma_{k+1}^j\right)$$

Estimated fire-sales losses EBA scenario



Monitoring systemic risk: The Indirect Contagion Index

Bipartite network of asset holdings



Indirect exposures across institutions through common asset holdings

Portfolio overlaps as drivers of price-mediated contagion

For $\alpha = 1$ and $\Psi_{\mu}(x) = \frac{x}{D_{\mu}}$ with $D_{\mu} = c \frac{ADV_{\mu}}{\sigma_{\mu}} \sqrt{\tau}$, the indirect loss of bank *i* resulting from deleveraging by other banks becomes:

$$\mathcal{L}^{i} = \sum_{j=1}^{N} \underbrace{\sum_{\mu=1}^{M} \frac{\Pi^{i\mu} \Pi^{j\mu}}{D_{\mu}}}_{\Omega_{ij}} \Gamma^{j} = \sum_{j=1}^{N} \Omega_{ij} \Gamma^{j},$$

where Ω_{ij} is the **liquidity-weighted overlap** between portfolios *i* and *j* (Cont & Wagalath 2013):

$$\Omega_{ij} = \sum_{\mu=1}^{M} \frac{\Pi^{i\mu} \Pi^{j\mu}}{D_{\mu}} \qquad D_{\mu} = \text{market depth for asset } \mu$$

 Ω_{ij} = exposure of marketable assets of *i* to deleveraging by *j*. \Rightarrow loss contagion = contagion process on network defined by $[\Omega_{ij}]$

Indirect contagion

The first round fire-sales losses across the banking system are thus given by

$$FLoss = \Omega\Gamma$$
.

When the liquidity-weighted overlap network is close to a 1-factor model

 $\Omega \approx \lambda_1 u u^{\top},$

then the first round fire sales loss of i is

$$\log(Floss^{i}) = \log(\lambda_{1}u_{i}\sum_{j=1}^{N}u_{j}\Gamma_{j}(\epsilon)),$$

and we expect a slope 1 when regressing the log fire-sales losses on the log ICI:

$$\log(Floss^{i}) = 1 \times \log(u_{i}) + \log(\lambda_{1}) + \log(\langle u, \Gamma(\epsilon) \rangle).$$

- Collect portfolio holdings Π^{i,μ} by asset class for each financial institution in the network, at the granularity level corresponding to bank stress tests.
- **②** Estimate a market depth parameter $D_{\mu} \propto \frac{ADV_{\mu}}{\sigma_{\mu}}$ for each asset class.

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- $\textbf{S} \ \text{Check that} \ \Omega_{ij} \geq 0 \ \text{and that} \ \Omega \ \text{is irreducible}.$
- Generative Compute the "Perron eigenvector" $u = (u_i, i = 1...N)$ of the matrix of liquidity-weighted overlaps Ω(Π) = ΠD⁻¹Π[⊤] (SVD of Π√D⁻¹).

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- Compute the "Perron eigenvector" $u = (u_i, i = 1...N)$ of the matrix of liquidity-weighted overlaps $\Omega(\Pi) = \Pi D^{-1} \Pi^{\top}$ (SVD of $\Pi \sqrt{D^{-1}}$).
- The Indirect Contagion Index is the Perron eigenvector, ICI = u, whose component ICI(i) = u_i provides a measure of centrality of the node i in the network whose links are weighted by the overlap matrix Ω.

Principal component analysis of portfolio holdings



Figure: European banking system: Eigenvalues of matrix of liquidity-weighted overlaps. Source: EBA (public)

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The Indirect Contagion Index (EBA 2016)



Component

The EU indirect contagion network (2016)



Portfolio overlaps, Ω_{ij} , across EU banks (EBA 2016)





Figure: Bank-level fire-sales losses regressed on the ICI.



Figure: Bank-level fire-sales losses regressed on the ICI.

Table: Regression of bank-level fire-sales losses on the Indirect Contagion Index for all banks.

	Round 1	Round 2	Round 3	Round 4	Total
Slope	0.684***	0.762***	0.594***	0.10	0.490 ***
	(0.072)	(0.052)	(0.047)	(0.168)	(0.040)
Intercept	10.85***	11.39***	11.12***	9.06***	11.4***
	(0.190)	(0.130)	(0.128)	(0.411)	(0.106)
n	51	49	32	16	51
adj. <i>R</i> ²	0.64	0.82	0.83	-0.04	0.74

Table: Regressing fire-sales losses on the ICI. *** denotes significance $p < 10^{-4}$.



Figure: Slope of the regression of fire-sales losses on the ICI, as a function of the shock size and market depth.



Figure: R^2 of the regression of fire-sales losses on the ICI, as a function of the shock size and market depth.

Robustness checks

Nominal overlaps. Perron eigenvector of

 $\Omega_{Nominal} = \Pi \Pi^{\top}.$

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Cosine Similarity. [Getmansky et al., 2016], Portfolio weights:

$$w_i := rac{1}{\sum_{\mu=1}^M \Pi^{i,\mu}} (\Pi^{i,1},\ldots,\Pi^{i,M})^{ op}.$$

Cosine similarity: Perron eigenvector of $\Omega_{C.S.}$ given by

$$\Omega_{C.S.}^{ij} = \frac{\langle w_i, w_j \rangle}{||w_i||_2||w_j||_2} \in [-1, 1].$$

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Size.

$$size = rac{(\Pi^1, \ldots, \Pi^N)}{||(\Pi^1, \ldots, \Pi^N)||_2},$$

where $\Pi^i := \sum_{\mu=1}^M \Pi^{i,\mu}$.

Similarity between overlap measures

	ICI	Nom. Ov.	Cos. Sim.	Size
ICI	1	0.68 (0.85)	- 0.13 (- 0.22)	0.60 (0.80)
Nom. Ov.		1	- 0.14 (-0.22)	0.78 (0.92)
Cos. Sim.			1	- 0.17 (-0.26)
Size				1

Table: Similarity between the various overlap measures: The bold numbers are rank-correlations (Kendall's τ), while the numbers in brackets are linear correlations (Spearman's ρ).



Liquidity-weighted overlaps



Component

Nominal overlaps



Component

$$\log_{10}(FSLoss^{i}) = b_1 \log_{10}(X) + b_0 + \epsilon$$

	ICI	Nominal overlap	Total Assets	Similarity
Slope	0.684***	0.742***	71.4***	-0.627**
	(0.072)	(0.089)	(14.9)	(0.295)
Intercept	10.85***	10.68***	-505***	8.49***
	(0.190)	(0.190)	(107)	(0.395)
n	51	51	51	51
adj. R ²	0.64	0.31	0.57	0.07

Table: Regression of bank losses on the Indirect Contagion Index and other measures (X) for all banks. First round only.

 $\log_{10}(FSLoss^{i}) = b_{1}\log_{10}(ICI) + b_{2}\log_{10}(N.Ov.) + b_{3}\log_{10}(Size) + b_{0} + \epsilon.$

Dependent Variable	Estimate	Std. dev.	p-value
ICI	0.22***	(0.062)	9.34E-4
Nominal Overlap	0.22***	(0.080)	5.97E-3
Size	22***	(7.09)	3.20E-3
Intercept	-147***	(51)	5.90E-3
	n = 51	adj. $R^2 = 0.84$	

Global systemically important banks

Indicator-based measurem	Table 1	
Category (and weighting)	Individual indicator	Indicator weighting
Cross-jurisdictional activity (20%)	Cross-jurisdictional claims	10%
	Cross-jurisdictional liabilities	10%
Size (20%)	Total exposures as defined for use in the Basel III leverage ratio	20%
Interconnectedness (20%)	Intra-financial system assets	6.67%
	Intra-financial system liabilities	6.67%
	Securities outstanding	6.67%
Substitutability/financial	Assets under custody	6.67%
institution infrastructure (20%)	Payments activity	6.67%
	Underwritten transactions in debt and equity markets	6.67%
Complexity (20%)	Notional amount of over-the-counter (OTC) derivatives	6.67%
	Level 3 assets	6.67%
	Trading and available-for-sale securities	6.67%

Figure: BCBS GSIB Indicator measurement approach. Source: Basel Committee on Banking Supervision (2013).

"Spillover"-ICI: Discount self-inflicted losses

Consider a portfolio network given by:

$$\Pi = \begin{pmatrix} 1000 & 0 & 0 & 0 & 0 & 0 \\ 100 & 1100 & 100 & 100 & 100 & 100 \end{pmatrix}^{\top}$$
$$D = (1000, 2000)^{\top}.$$

- Compute $\Omega = \Pi D^{-1} \Pi^{\top}$, as before.
- Compute the principal (largest) eigenvalue and the corresponding eigenvector (the "Perron eigenvector") of Ω₀ := Ω diag(Ω₁₁,...,Ω_{NN}).

ICI and ICI_0



Figure: Illustrative example showing how the ICI_0 discounts self-inflicted losses compared to the losses caused for other participants relative to the ICI.

ICI_0



Bank

Scenario design

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Motivation

- Currently, the starting point for stress scenario design is often based on macroeconomic- and broader financial developments.
- The stress test scenario is often defined in terms of macroeconomic variables, which banks map to specific risk factors.
- Portfolio holdings and exposures do not play a large role, if any, in constructing the scenario.

Motivation

- Currently, the starting point for stress scenario design is often based on macroeconomic- and broader financial developments.
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Reverse stress testing and scenario design: First collect portfolio holdings and identify the main exposures/vulnerabilities. This has two advantages:

- For a given scenario, we can assess how "close" it is to a worst-case scenario in terms of contagion effects.
- The scenario can be designed such that particular weaknesses of the system are tested. This ensures that the scenario is "relevant".
Worst-case contagion scenario

Assume that the deleveraging of institutions is proportional to their resilience $R_i \in [0, 1]$. The weakest bank has resilience $R_i = 1$; a bank which is "fully" resilient and generates no fire sales has $R_i = 0$.

Worst-case contagion scenario

Assume that the deleveraging of institutions is proportional to their resilience $R_i \in [0, 1]$. The weakest bank has resilience $R_i = 1$; a bank which is "fully" resilient and generates no fire sales has $R_i = 0$.

View Ω as a map from deleveraging proportions/shock to fire-sales losses:

$$\Omega: [0,1]^{\mathsf{N}} \mapsto \mathbb{R}^{\mathsf{N}}_+.$$

We want to find the scenario which maximizes

$$\max_{||x||_2 \leq 1} \left\{ \mathbf{1}^\top \Omega x \right\} = \max_{||x||_2 \leq 1} \left\{ f^\top x \right\},$$

where $f := \mathbf{1}^{\top} \Omega R$. The worst-case scenario, which follows immediately from Cauchy-Schwarz, is

$$x^* = \frac{f}{||f||_2}.$$

EBA 2016



Estimated fire-sales losses EBA scenario



Worst-case fire-sales losses



Ratio of EBA FSLoss to worst-case FSLoss



Further work

The problem

$$\max_{|\mathbf{x}||_2 \le 1} \left\{ \mathbf{1}^\top \Omega \mathbf{x} \right\} \tag{1}$$

only looks at the fire-sales losses. It (i) ignores losses suffered on illiquid assets, and (ii) implicitly assumes a leverage targeting behaviour instead of a threshold behaviour.

Further work

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Ideally, we would like to find scenarios $\epsilon \in [0,1]^{M+K}$ as shocks to asset classes, that maximize

$$\max_{\|\epsilon\|_2 \le 1} \mathbf{1}^\top A \epsilon + \mathbf{1}^\top \Omega \Gamma(A \epsilon), \tag{2}$$

where $A = (\Theta, \Pi)$, $\Gamma : \mathbb{R}^N \to \mathbb{R}^N$ is the threshold deleveraging function, and ϵ is potentially subject to further restrictions. This is a concave minimization.

Conclusions

- Overlapping portfolios give rise to an indirect contagion network. Under stress, the risk of a portfolio thus depends on the distress that similar portfolio-holders suffer.
- The indirect contagion index predicts fire-sales losses well, and can be used to quantify the systemicness of institutions.

Conclusions

- Overlapping portfolios give rise to an indirect contagion network. Under stress, the risk of a portfolio thus depends on the distress that similar portfolio-holders suffer.
- The indirect contagion index predicts fire-sales losses well, and can be used to quantify the systemicness of institutions.
- From the liquidity-weighted overlap network, we can derive a "worst-case" contagion scenario via a simple optimisation problem. This can be used both for benchmarking current stress scenarios, and for designing relevant future scenarios.
- The worst-case contagion scenario leads to a "perfect-storm" contagion, where the weaknesses of the system are specifically targeted.

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